$\begin{array}{c} {\rm MATH4220~PDE-Quiz~1~(10~points)} \\ {\rm February~18,~2016} \\ {\rm (in~class)} \end{array}$

1. (5 points) For each of the following equations, state the order, type and whether it is nonlinear, linear inhomogeneous, or linear homogeneous:

$$(1) \partial_t u - \partial_x^2 u + 1 = 0$$

$$(2) \ \partial_t^2 u - \partial_x^2 u + u^2 = 0$$

$$(3) \ \partial_{xy}^2 u = \sin(4x)$$

$$(4) 2\partial_x^2 u + \partial_{xy}^2 u + \partial_y^2 u = 0$$

2. (5 points) Solve the equation $\partial_x u + x \partial_y u = 0$ with the following two conditions:

(a)
$$u(0,y) = y^2$$

(b)
$$u(x,0) = x^2$$